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$$\nabla^2 u_i + \frac{1}{1-2\nu} \frac{\partial \theta}{\partial x_i} + \frac{2\nu}{1-2\nu} \theta \frac{\partial \ln E}{\partial x_i} + \frac{\partial \ln E}{\partial x_j} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) = 0 \quad (3)$$

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v [2].

$$E = E(T), \quad \nu = const$$

$$\alpha = \alpha(T)$$

$$\nabla^2 u_i + \frac{1}{1-2\nu} \frac{\partial \theta}{\partial x_i} - \frac{2(1+\nu)}{1-2\nu} \frac{\partial}{\partial x_i} \left( \int_0^T \alpha(T) dt \right) + \frac{1}{E} \frac{\partial E}{\partial x_j} \left[ \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} + \frac{2\nu}{1-2\nu} \theta \delta_{ij} - \frac{2(1+\nu)}{1-2\nu} \int_0^T \alpha(T) dt \delta_{ij} \right] = 0; \quad (4)$$

$$\left[ \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) + \frac{\nu}{1-2\nu} \theta \delta_{ij} \right] n_j = \frac{1+\nu}{E} q_i(x_s) + \frac{1+\nu}{1-2\nu} n_i \int_0^T \alpha(T) dT. \quad (5)$$

[3]

$$\frac{1}{E} \frac{\partial E}{\partial x_j} = \frac{1}{E} \frac{dE}{dT} \frac{\partial T}{\partial x_j} = \chi Q(T) \frac{\partial T}{\partial x_j} = \chi B_j,$$

(1)

$$\nabla^2 u_i + \frac{1}{1-2\nu} \frac{\partial \theta}{\partial x_i} - \frac{2(1+\nu)}{1-2\nu} \frac{\partial}{\partial x_i} \left( \int_0^T \alpha(T) dt \right) + \chi B_j \left[ \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} + \frac{2\nu}{1-2\nu} \theta \delta_{ij} - \frac{2(1+\nu)}{1-2\nu} \int_0^T \alpha(T) dt \delta_{ij} \right] = 0. \quad (6)$$

[1],

$$u_i(x_s), \quad i = 1, 2, 3,$$

$$(\lambda + \mu) \frac{\partial \theta}{\partial x_i} + \mu \nabla^2 u_i + \theta \frac{\partial \lambda}{\partial x_i} + \frac{\partial \mu}{\partial x_i} + \rho F_i = 0 \quad (1)$$

$$\left[ \lambda \frac{\partial u_k}{\partial x_k} \delta_{ij} + \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right] n_j = q_i(x_s). \quad (2)$$

$$\lambda = \frac{\nu E}{(1+\nu)(1-2\nu)},$$

$$\mu = G = \frac{E}{2(1+\nu)}, \quad \nu \text{ ó } \quad (4), (5)$$

$$\theta = \frac{\partial u_k}{\partial x_k} \text{ ó}$$

$$u_i = u_i^0 + \sum_{k=1}^{\infty} \chi^k u_i^k. \quad (7)$$

$n_j$  ó

$q_i(x_s)$  ó

$\rho$  ó  $F_i$  ó

$u_i^0$  :

$$\nu = const (\neq 0,5), \quad E = E(x_s).$$

$$\nabla^2 u_i^0 + \frac{1}{1-2\nu} \frac{\partial \theta^0}{\partial x_i} = \frac{2(1+\nu)}{1-2\nu} \frac{\partial}{\partial x_i} \left( \int_0^T \alpha(T) dt \right), \quad \alpha(T) = \alpha_0 (1 + \gamma T), \quad (16)$$

$$- \left[ \frac{1}{2} \left( \frac{\partial u_i^0}{\partial x_j} + \frac{\partial u_j^0}{\partial x_i} \right) + \frac{\nu}{1-2\nu} \theta \delta_{ij} \right] n_i = \quad (8)$$

$$= \frac{1+\nu}{E} q_i(x_s) + \frac{1+\nu}{1-2\nu} n_i \int_0^T \alpha(T) dt \quad \Delta W = a \left( T + \frac{T^2}{2} \gamma \right), \quad (17)$$

$$u_i^k, \quad k = 1, 2, \dots \quad a = \alpha_0 \frac{1+\nu}{1-\nu}.$$

$$\nabla^2 u_i^k + \frac{1}{1-2\nu} \frac{\partial \theta^k}{\partial x_i} = -B_j \left[ \frac{\partial u_i^{k-1}}{\partial x_j} + \frac{\partial u_j^{k-1}}{\partial x_i} + \frac{2\nu}{1-2\nu} \theta^{k-1} \delta_{ij} \right], \quad \lambda(T) = \lambda_0 (1 - kT), \quad (18)$$

$$\left[ \frac{1}{2} \left( \frac{\partial u_i^k}{\partial x_j} + \frac{\partial u_j^k}{\partial x_i} \right) + \frac{\nu}{1-2\nu} \theta \delta_{ij} \right] n_j = 0. \quad (9)$$

$$\sigma_{ij} = \frac{E(T)}{1+\nu} \times \quad (18)$$

$$\times \left\{ \left[ \frac{1}{2} \left( \frac{\partial u_i^0}{\partial x_j} + \frac{\partial u_j^0}{\partial x_i} \right) + \frac{\nu}{1-2\nu} \frac{\partial u_k^0}{\partial x_k} \delta_{ij} - \frac{1+\nu}{1-2\nu} \int_0^T \alpha(T) dt \delta_{ij} \right] + \right. \quad T = \frac{1}{k} \left( 1 - \sqrt{1 - \frac{2k}{\lambda_0} T^*} \right). \quad (19)$$

$$\left. \sum_{k=1}^{\infty} \chi^k \left[ \frac{1}{2} \left( \frac{\partial u_i^k}{\partial x_j} + \frac{\partial u_j^k}{\partial x_i} \right) + \frac{\nu}{1-2\nu} \frac{\partial u_k^k}{\partial x_k} \delta_{ij} \right] \right\}. \quad (19) \quad \Delta W = abT - acT^*. \quad (20)$$

$$b = 1 + \frac{\gamma}{k}; c = \frac{\gamma}{k\lambda_0}.$$

$$\Delta W = -\frac{ab}{4\pi} \int \frac{T(y)}{r} \Delta \left( \frac{1}{r} \right) dV_y - \quad (21)$$

$$\frac{ac}{4\pi} \int \frac{dT^*}{dn_y} \Delta \left( \frac{r}{2} \right) + T^*(y) \Delta \left( \frac{\cos \varphi}{2} \right) dS_y$$

$$W = -\frac{ab}{4\pi} \int \frac{T(y)}{r} dV_y - \frac{ac}{4\pi} \int \left[ \frac{dT^*}{dn_y} \left( \frac{r}{2} \right) - T^*(y) \frac{\cos \varphi}{2} \right] dS_y, \quad (22)$$

(13)

$$2\pi T(x) = \int_s \left( \frac{dT}{dn_y} \frac{1}{r} + T(y) \frac{\cos \varphi}{r^2} \right) dS_y, \quad (11)$$

$$r = |y - x|, \quad x \text{ ó } y,$$

$$\bar{r} = \frac{\cos \varphi}{n_y}.$$

$$u_i^0 = u_i^u + u_i^T, \quad (12)$$

$$u_i^T = \frac{\partial W}{\partial x_i}. \quad (13)$$

$$\sigma_{ij}^0 = \sigma_{ij}^u + \sigma_{ij}^T. \quad (14)$$

$$\sigma_{ij}^u \quad u_i^u, \quad \sigma_{ij}^T \quad u_i^T. \quad (8)$$

$$\Delta W = \frac{1+\nu}{1-\nu} \int_0^T \alpha(T) dT. \quad (15)$$

$$\sigma_{ij}^T = \frac{E}{1+\nu} \left( \frac{\partial^2 W}{\partial x_i \partial x_j} - \Delta W \delta_{ij} \right). \quad (24)$$

$$\sigma_{ij}^T(x) = \frac{\alpha_0 E}{1-\nu} \left[ 4\pi T(x) \delta_{ij} - \frac{b}{4\pi} \int \frac{T(y)}{r^3} (3\beta_i \beta_j - \delta_{ij}) dV_y + \right. \\ \left. + \frac{C}{8\pi} \int \left[ \frac{dT^*}{dn_y} \left( -\frac{\beta_i + \delta_{ij}}{r} \right) + T^*(y) \frac{1}{r^2} [n_i(y) \beta_j + n_j(y) \beta_i - \right. \right. \\ \left. \left. - 3\beta_i \beta_j \cos \varphi - \cos \varphi \delta_{ij} \right] dS_y \right]. \quad (25)$$

$$\sigma_{ij}^T(\mathbf{x})_s = \frac{\alpha_0 \mathbf{E}}{1-\nu} \left\langle -\frac{\mathbf{b}}{2\pi} \left[ 4\pi \mathbf{T}(\mathbf{x}) \left[ \delta_{ij} - \frac{\mathbf{n}_i(\mathbf{x})\mathbf{n}_j(\mathbf{x})}{2} \right] + \int_V \mathbf{T}(\mathbf{y}) \frac{3\beta_i\beta_j - \delta_{ij}}{r^3} dV_y \right] + \frac{\mathbf{C}}{8\pi} \left[ 2\pi m_i(\mathbf{x})\mathbf{n}_j(\mathbf{x}) - 2\pi \delta_{ij} \right] \mathbf{T}^*(\mathbf{x}) + \int_S \left[ \frac{d\mathbf{T}^*}{dn} \left( -\frac{\beta_i + \delta_{ij}}{r} \right) + \mathbf{T}^*(\mathbf{y}) \frac{1}{r^2} (\mathbf{n}_i(\mathbf{y})\beta_j + \mathbf{n}_j(\mathbf{y})\beta_i - 3\beta_i\beta_j \cos \varphi - \cos \varphi \delta_{ij}) \right] dS_y \right\rangle. \quad (26)$$

$$\rho_i^T(\mathbf{x}) = -\sigma_{ij}^T(\mathbf{x})_s \cdot \mathbf{n}_j(\mathbf{x}), \quad (27)$$

$$v_i(\mathbf{x}) + \frac{1}{4\pi(1+\nu)} \times \int_S v_k(\mathbf{y}) \left\{ (1-2\nu) [\delta_{ik} \cos \psi + \mathbf{n}_k(\mathbf{x})\beta_i - \mathbf{n}_i(\mathbf{x})\beta_k] + 3\beta_i\beta_j \cos \psi \right\} \cdot \frac{1}{r^2} dS_y = p_i(\mathbf{x}) + p_i^T(\mathbf{x}). \quad (28)$$

$$v_i(\mathbf{x}) + \frac{1}{4\pi(1+\nu)} \times \int_S v_k(\mathbf{y}) \left\{ (1-2\nu) [\delta_{ik} \cos \psi + \mathbf{n}_k(\mathbf{x})\beta_i - \mathbf{n}_i(\mathbf{x})\beta_k] + 3\beta_i\beta_j \cos \psi \right\} \cdot \frac{1}{r^2} dS_y = p_i(\mathbf{x}) + p_i^T(\mathbf{x}). \quad (28)$$

$$\Delta U_i^k + \frac{1}{1-2\nu} \frac{\partial^2 U_j}{\partial x_i \partial x_j} = -\frac{2(1+\nu)}{E^2} \frac{d\mathbf{E}}{dT} \frac{\partial \mathbf{T}}{\partial x_j} \cdot \sigma_{ij}^0. \quad (27)$$

$$\mathbf{u}_i^{(k)} = \mathbf{u}_i^u + \mathbf{u}_i^N, \quad (28)$$

$$\mathbf{u}_i^N = -\int_V \left[ \frac{2(1+\nu)}{E^2} \frac{d\mathbf{E}}{dT} \frac{\partial \mathbf{T}}{\partial x_p} \right] U_{ij} dV_y, \quad (29)$$

$$\mathbf{u}_i^N = -\frac{(1+\nu)^2}{4\pi(1-\nu)} \int_V \left( \frac{1}{E^2} \cdot \frac{d\mathbf{E}}{dT} \cdot \frac{\partial \mathbf{T}}{\partial x_p} \cdot \sigma_{jp}^0 \right) \cdot \frac{3-4\nu \cdot \delta_{ij} - \beta_i\beta_j}{E \cdot r} dV_y. \quad (30)$$

$$\sigma_{ij}^{(k)} = \sigma_{ij}^u + \sigma_{ij}^N. \quad (31)$$

$$\sigma_{ij}^u \quad \mathbf{u}_i^u \quad (4).$$

$$\sigma_{ij}^N \quad (5).$$

$$\sigma_{ij}^N(\mathbf{x}) = a_i \mathbf{E}(\mathbf{T}) \int_V \rho_k(\mathbf{y}) \frac{d\mathbf{E}}{dT} \cdot \frac{1}{E^3(\mathbf{T})} \left\{ \frac{1}{r^2} [(1-2\nu) \cdot (\delta_{ik}\beta_j + \delta_{kj}\beta_i - \delta_{ij}\beta_k) + 3\beta_i\beta_j\beta_k] - \frac{d\mathbf{E}}{dT} \cdot \frac{1}{2E^2(\mathbf{T}) \cdot r} \right\} \cdot \left\{ \frac{\partial \mathbf{T}}{\partial x_i} [(3-4\nu) \cdot \delta_{jk} + \beta_j\beta_k] + \frac{\partial \mathbf{T}}{\partial x_j} [(3-4\nu) \cdot \delta_{ik} + \beta_i\beta_k] \right\}_y. \quad (32)$$

$$\frac{2}{1-2\nu} \cdot \delta_{ij} \sum_{m=1}^3 \frac{\partial \mathbf{T}}{\partial x_m} [(3-4\nu) \cdot \delta_{mk} + \beta_m\beta_k] \left\langle dV, \right. \\ \left. a_i = \frac{1+\nu}{4\pi(1-\nu)}; \rho_k(\mathbf{y}) = \frac{\partial \mathbf{T}}{\partial x_p} \sigma_{pk}^0. \right. \quad (32)$$

$$\sigma_{ij}^N(\mathbf{x})$$

$$f_i^N(\mathbf{x}) \quad f_i^N(\mathbf{x}) = -\sigma_{ij}^N(\mathbf{x}) \cdot \mathbf{n}_j, \quad (18)$$

$$f_i(\mathbf{x}).$$

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