

3. 6 2, 1997 ó . 936
 - 95.
 - 4. 5.03.01698 ö , 1998 ó 178
 2. ö ó ö - 5.
 6 , 1978,
 1. 6 ó . 1426150.
 - 6. (5.03.01698) ó
 / - , 1998 ó 244 , 1999 ó 157 .
 2.
 1974 ó 560 .
 624.015

[1,3],
 [2].

$$\sigma_x = 2G \frac{\partial U}{\partial x} + \lambda \left(\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial W}{\partial z} \right);$$

$$\tau_{yx} = G \left(\frac{\partial U}{\partial y} + \frac{\partial V}{\partial x} \right);$$

$$\tau_{zx} = G \left(\frac{\partial U}{\partial z} + \frac{\partial W}{\partial x} \right);$$

[4]

$$\frac{\partial \sigma_x}{\partial x} + \frac{\partial \tau_{xy}}{\partial y} + \frac{\partial \tau_{xz}}{\partial z} = 0,$$

$$2G \frac{\partial^2 U}{\partial x^2} + \lambda \frac{\partial}{\partial x} \left(\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial W}{\partial z} \right) + G \frac{\partial^2 U}{\partial y^2} + G \frac{\partial^2 V}{\partial y \partial x} + \frac{\partial^2 U}{\partial z^2} + G \frac{\partial^2 W}{\partial z \partial x} = 0;$$

[5].

$$G \frac{\partial^2 U}{\partial x^2} + G \frac{\partial^2 U}{\partial x^2} + \lambda \frac{\partial}{\partial x} \theta + G \frac{\partial^2 U}{\partial y^2} + G \frac{\partial^2 V}{\partial y \partial x} + \frac{\partial^2 U}{\partial z^2} + G \frac{\partial^2 W}{\partial z \partial x} = 0;$$

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$$G \left(\frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} + \frac{\partial^2 U}{\partial z^2} \right) = G \nabla^2 U; \frac{\partial}{\partial x} \left(\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial W}{\partial z} \right) = G \frac{\partial}{\partial x} \theta;$$

$$: (\lambda + G) \frac{\partial}{\partial x} \theta + G \nabla^2 U = 0;$$

$$(\lambda + G) \frac{\partial}{\partial x} \theta + G \nabla^2 U = 0;$$

$$(\lambda + G) \frac{\partial}{\partial y} \theta + G \nabla^2 V = 0; \tag{1}$$

$$(\lambda + G) \frac{\partial}{\partial z} \theta + G \nabla^2 W = 0,$$

$$\nabla^2 U, \nabla^2 V, \nabla^2 W$$

$$(\lambda + G) \left[\left(\frac{1}{\Delta x^2} (U_{i+1jk} + U_{i-1jk} - 2U_{ijk}) + \frac{1}{\Delta x \Delta y} (V_{i+1jk} + V_{i-1j-1k} - V_{i+1j-1k} - V_{i-1j+1k}) + \frac{1}{\Delta x \Delta y} (W_{i+1jk+1} + W_{i-1jk-1} - W_{i+1jk-1} - W_{i-1jk+1}) \right) \right] + G \left[\frac{1}{\Delta x^2} (U_{i+1jk} + U_{i-1jk} - 2U_{ijk}) + \frac{1}{\Delta y^2} (U_{ij+1k} + U_{ij-1k} - 2U_{ijk}) + \frac{1}{\Delta z^2} (U_{ijk+1} + U_{ijk-1} - 2U_{ijk}) \right] J = 0;$$

$$U_{ijr} = \frac{1}{G_1} \{ (\lambda + G) \left[\left(\frac{1}{\Delta x^2} (U_{i+1jk} + U_{i-1jk}) + \frac{1}{\Delta x \Delta y} (V_{i+1jk} + V_{i-1j-1k} - V_{i+1j-1k} - V_{i-1j+1k}) + \frac{1}{\Delta x \Delta y} (W_{i+1jk+1} + W_{i-1jk-1} - W_{i+1jk-1} - W_{i-1jk+1}) \right) \right] + G \left[\frac{1}{\Delta x^2} (U_{i+1jk} + U_{i-1jk}) + \frac{1}{\Delta y^2} (U_{ij+1k} + U_{ij-1k}) + \frac{1}{\Delta z^2} (U_{ijk+1} + U_{ijk-1}) \right] \} = 0;$$

$$V_{ijk} = \frac{1}{G_1} \{ (\lambda + G) \left[\left(\frac{1}{\Delta x \Delta y} (U_{i+1j+1k} + U_{i-1j-1k} - U_{i+1j-1k} - U_{i-1j+1k}) + \frac{1}{\Delta y^2} (V_{ij+1k} + V_{ij-1k}) + \frac{1}{\Delta y \Delta z} (W_{ij+1k+1} + W_{ij-1k-1} - W_{ij+1k-1} - W_{ij-1k+1}) \right) \right] + G \left[\frac{1}{\Delta x^2} (V_{i+1jk} + V_{i-1jk}) + \frac{1}{\Delta y^2} (V_{ij+1k} + V_{ij-1k} - 2V_{ijk}) + \frac{1}{\Delta z^2} (V_{ijk+1} + V_{ijk-1}) \right] \} = 0;$$

$$W_{ijk} = \frac{1}{G_1} \{ (\lambda + G) \left[\left(\frac{1}{\Delta x \Delta z} (U_{i+1jk+1} + U_{i-1jk-1} - U_{i+1jk-1} - U_{i-1jk+1}) + \frac{1}{\Delta y \Delta z} (V_{ij+1k+1} + V_{ij-1k-1} - V_{ij+1k-1} - V_{ij-1k+1}) \right) \right] + \frac{1}{\Delta z^2} (W_{ijk+1} + W_{ijk-1}) + G \left[\frac{1}{\Delta x^2} (W_{i+1jk} + W_{i-1jk}) + \frac{1}{\Delta y^2} (W_{ij+1k} + W_{ij-1k}) + \frac{1}{\Delta z^2} (W_{ijk+1} + W_{ijk-1}) \right] \} = 0$$

$$G_1 = 0,5 \left(\frac{\lambda + G}{\Delta x^2} + \frac{G}{\Delta x^2} + \frac{G}{\Delta y^2} + \frac{G}{\Delta z^2} \right).$$

(2).

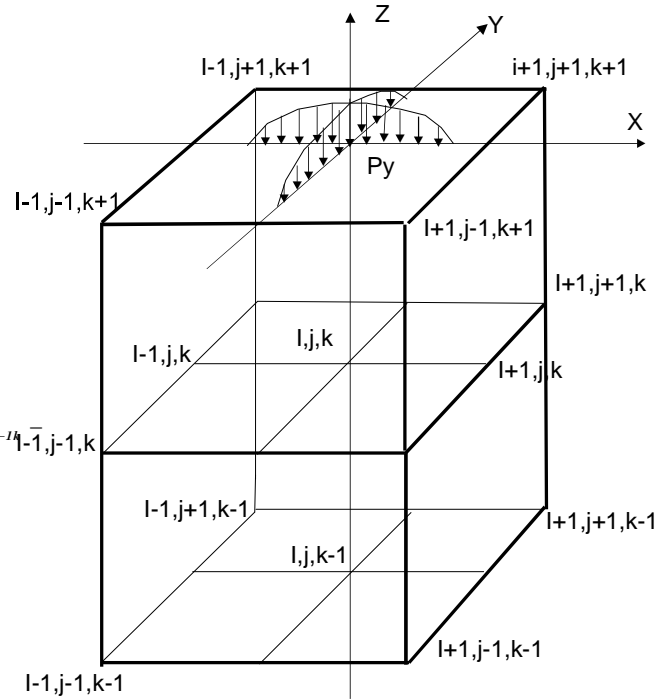
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(2)

1. XOZ:

$$\sigma_y = 0; \tau_{xy} = \tau_{yz} = 0;$$

$$t_{xy} = G \gamma_{xy} = G \left(\frac{\partial V}{\partial x} + \frac{\partial U}{\partial y} \right) = 0$$



$$G \left(\frac{U_{ijk} - U_{ij-1k} + V_{i+1jk} - V_{i-1jk}}{\Delta y} \right) = 0;$$

$$U_{ijk} = -\frac{\Delta y}{2 \Delta x} (V_{i+1jk} - V_{i-1jk}) + U_{ij-1k}$$

$$\tau_{xy} = G \gamma_{xy} = G \left(\frac{\partial W}{\partial y} + \frac{\partial V}{\partial z} \right) = 0;$$

$$G \left(\frac{V_{ijk+1} - V_{ijk-1} + W_{ijk} - W_{ij-1k}}{2 \Delta z} + \frac{W_{ijk} - W_{ij-1k}}{\Delta y} \right) = 0;$$

(7)

$$W_{ijk} = -\frac{\Delta y}{2 \Delta z} (V_{ijk+1} - V_{ijk-1}) + W_{ij-1k};$$

$$\sigma_y = 2G \xi_y + \lambda \theta = 0$$

$$\xi_y = \frac{\partial V}{\partial y}; \theta = \xi_x + \xi_y + \xi_z;$$

$$\sigma_y = 2G \frac{\partial V}{\partial y} + \lambda \left(\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial W}{\partial z} \right);$$

$$\sigma_y = 2G \left[\frac{V_{ijk} - V_{ij-1k}}{\Delta y} + \frac{\mu}{1 - 2\mu} \left(\frac{U_{i+1jk} - U_{i-1jk}}{2 \Delta x} + \frac{V_{ijk} - V_{ij-1k}}{\Delta y} + \frac{W_{ijk+1} - W_{ijk-1}}{2 \Delta z} \right) \right] = 0;$$

$$V_{ijk} = \frac{\mu \Delta y}{(1 - \mu)} \left(\frac{U_{i+1jk} - U_{i-1jk}}{2 \Delta x} + \frac{W_{ijk+1} - W_{ijk-1}}{2 \Delta z} + \frac{V_{ij-1k}}{\Delta y} \right) + \frac{(1 - 2\mu) V_{ij-1k}}{(1 - \mu)};$$

(8)

$$\sigma_y = -P_y.$$

(9)

$$P_y = -k P_{max} \left(\frac{x^2}{2a^2} + \frac{y^2}{2b^2} - 1 \right); (A)$$

(10)

$$V_{ijk} = -\frac{\mu \Delta y}{(1 - \mu)} \left(\frac{U_{i+1jk} - U_{i-1jk}}{2 \Delta x} + \frac{W_{ijk+1} - W_{ijk-1}}{2 \Delta z} + \frac{V_{ij-1k}}{\Delta y} \right) + \frac{1 - 2\mu}{1 - \mu} V_{ij-1k} - P_y \frac{(1 - 2\mu)(1 + \mu)}{E(1 - \mu)\Delta y};$$

3.
$$U_{ijk} = 0; V_{ijk} = 0; W_{ijk} = 0 \quad (11)$$

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1. , , // , - 1971. - 4.

624.151

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[1]

[2].

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1.

$$\sigma_x = \frac{1-\mu_0^2}{\mu_1} E_{x(y)} \varepsilon_x + \frac{\mu_0(1+\mu_0)}{\mu_1} E_{y(y)} \varepsilon_y ,$$

$$\sigma_y = \frac{\mu_0(1+\mu_0^2)}{\mu_1} E_{x(y)} \varepsilon_x + \frac{1-\mu_0^2}{\mu_1} E_{y(y)} \varepsilon_y , \quad (1)$$

$$\tau_{xy} = \frac{1}{4(1+\mu_0)} [E_{x(y)} + E_{y(y)}] \gamma_{xy} ,$$

$$\mu_1 = 1 - \mu_0^2 (2\mu_0 + 3) .$$

2.

$$\varepsilon_x = \frac{\partial u}{\partial x} ;$$

$$\varepsilon_y = \frac{\partial v}{\partial y} \quad (2)$$

2. . . . // , 1972. -

18.- . 8 -11.

3. . . . 1973. - 246 .

4. 2.02-83. 05.12.83.

-15-74. 01.01.85/ . 6 1985.- 40 . () .

5. . . . // -1978.- 10.- . 31-33.

$$\gamma_{xy} = \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} .$$

3.

$$\frac{\partial \sigma_x}{\partial x} + \frac{\partial \tau_{xy}}{\partial y} + X = 0 ;$$

$$\frac{\partial \tau_{xy}}{\partial x} + \frac{\partial \sigma_y}{\partial y} + Y = 0 . \quad (3)$$

(1) (2),

() :

[3]:

$$\frac{1-\mu_0^2}{\mu_1} E_{x(y)} \frac{\partial^2 u}{\partial x^2} + \frac{E_{x(y)} + E_{y(y)}}{4(1+\mu_0)} \frac{\partial^2 u}{\partial y^2} +$$

$$+ \left[\frac{\mu_0(1+\mu_0)}{\mu_1} E_{y(y)} + \frac{\mu_0(1+\mu_0)}{\mu_1} E_{x(y)} \right] \frac{\partial^2 v}{\partial x \partial y} +$$

$$\frac{\mu_0(1-\mu_0)}{\mu_1} \frac{\partial E_{x(y)}}{\partial y} \frac{\partial v}{\partial x} + \frac{(1-\mu_0^2)}{\mu_1} \frac{\partial E_{y(y)}}{\partial y} \frac{\partial u}{\partial y} = 0$$

$$\frac{E_{x(y)} + E_{y(y)}}{4(1+\mu_0)} \frac{\partial^2 v}{\partial x^2} + \frac{1-\mu_0^2}{\mu_1} E_{y(y)} \frac{\partial^2 v}{\partial y^2} +$$

$$+ \left[\frac{E_{x(y)} + E_{y(y)}}{4(1+\mu_0)} + \frac{\mu_0(1+\mu_0)E_{x(y)}}{\mu_1} \right] \frac{\partial^2 u}{\partial x \partial y} + \quad (4)$$

$$\frac{\mu(1+\mu_0)}{\mu} \frac{\partial E_{x(y)}}{\partial y} \frac{\partial u}{\partial x} + \frac{(1-\mu_0^2)}{\mu_1} \frac{\partial E_{y(y)}}{\partial y} \frac{\partial v}{\partial y} = 0 ;$$

(4)

$\Delta x \Delta y .$